

# **Solving the Puzzle of IRR Equation**

## **Choosing the Right Solution to Measure Investment Success**

by

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